

Flexures

ME EN 7960 – Precision Machine Design
Topic 12



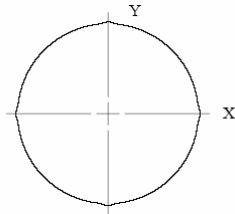
General

- Flexural Bearings are widely used in practice
- Application range from:
 - Flip-top on a shampoo bottle
 - Piezo-beams on a scanning tunneling microscope
- Because of the bending stresses created in the flexure, great care needs to be taken when designing these bearings
- Flexures, if designed properly, are very stiff & robust, light weight, maintenance free, and provide nanometer to sub-nanometer-level guiding precision (simple designs induce cosine runout errors)
- They are frictionless and do neither require lubricants nor air films



Friction in Conventional Linear Bearings

- Static friction approximately equals dynamic friction at low speeds, so stick slip is often minimized
- For heavily loaded tables, static friction is still significantly greater than dynamic friction
 - Errors will appear at velocity crossovers:



Source: Alexander Slocum, *Precision Machine Design*

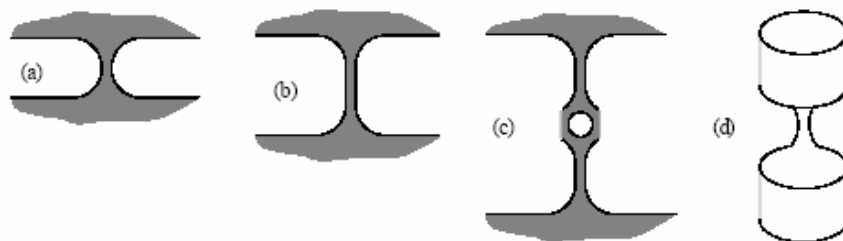
Bearing	“Dimple” size
Sliding contact	10 – 20 μm
Recirculating rolling element	3 – 5 μm
Crossed rollers	1 – 2 μm
Hydrostatic or aerostatic	0 μm



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Monolithic Design



Source: Alexander Slocum, *Precision Machine Design*

- Most accurate
- Sometimes difficult to machine:
 - Abrasive water jet machining is an economical way to cut non-critical areas (links)
 - Wire EDM can be used for precision cuts in critical hinge areas



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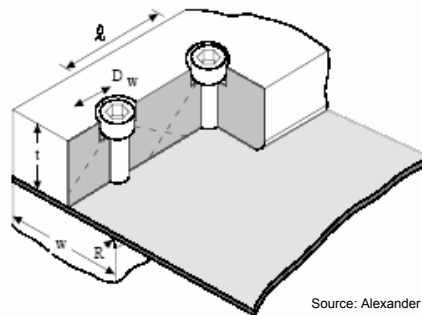
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Monolithic Design

- May require localized heat treating of the material in the flexure
- Applications include flexural couplings, mirror mounts, STM's, and many others
- Size is about 20 times the range of motion



Clamp Design



Source: Alexander Slocum, *Precision Machine Design*

- Nanometer accuracy and better can be obtained if the bolted joint is properly designed
 - Rounded edges
 - Bolt cones-of-action overlap



Clamp Design

- Easy to assemble from annealed parts and hardened spring steel
 - Careful when tightening bolts, as the torque can twist the flexure
 - Lubricated thrust washers can help
- Care is required to make sure residual stresses don't create asymmetries that create parasitic error motions
 - Cut spring metal with EDM or WaterJet
 - Use dual lubricated washers under bolt heads and guides for clamp plates
- Applications include wafer steppers, mirror mounts, and many others
- Size is about 10 times the range of motion



Performance

Speed and acceleration limits

- Limited only by yield strength and design

Range of motion

- Typically used for motions less than a few millimeters
- Monolithic designs: flexure length/motion = 20 or more
- Clamped designs: flexure length/motion = 5-10

Applied loads

- Design goal is to obtain load capacity with minimum spring constant

Repeatability

- Axial: limited only by the drive system
- Lateral: less than nanometers for monolithic designs



Performance

Resolution

- Axial: limited only by the drive system

Preload

- Inherently preloaded

Stiffness

- The greater the motion and the lower the spring rate, the less the stiffness
- Theory of elasticity or finite element analysis yields very accurate predictions of performance
- Flexures often have low transverse stiffness, so they are more susceptible to parasitic forces

Vibration and shock resistance

- Very good



Performance

Damping capability

- Material damping only (2-5%)
- Damping mechanisms (constrained layer dampers) can be used to obtain high damping

Accuracy

- Axial: limited only by the drive system
- Lateral: can be less than nanometers for monolithic designs
- Depends on how well the bearing was assembled or machined
- Even if there is a small off-axis error motion associated with the primary motion:
 - The error motion is usually very predictable and highly repeatable



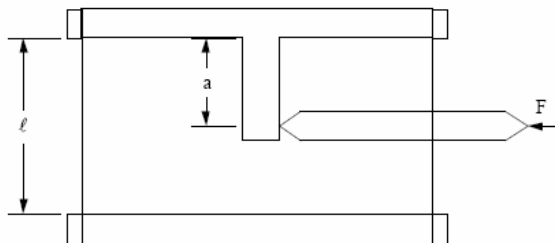
Performance

- Flexural bearings cannot attain perfect motion because of:
 - Variation in spring strength
 - Elastic modulus varies with rolling direction in steels
 - Variation in spring geometry
 - Overall inaccuracies of manufacture
 - Bending of the bearing in an unintended manner
 - Bending of structure
 - External applied loads (e.g., gravity and the manner in which the actuation force is applied)



Performance

- The most common errors are the pitch angle and vertical motion
 - They accompany linear motion in a four bar linkage flexure
- For small displacements, the errors are a function of:



Source: Alexander Slocum, *Precision Machine Design*



Performance

- The distance moved x
- The length of the springs l
- The spring thickness t
- The platform length b
- The distance of force application a above the fixed end of the springs

$$\theta_{pitch} = \left(\frac{6(l-2a)t^2}{3b^2l - 2t^2l + 6at^2} \right) \left(\frac{x}{l} \right) \quad \delta_{vertical} \approx \frac{x^2}{2l}$$

- At $a = l/2$ there is no pitch error.



Performance

- If the force is applied at a point other than halfway between the platforms:
 - A bending moment is generated which causes a pitch error to occur
- The pitch errors caused by the difference in spring length and difference in platform length are respectively:

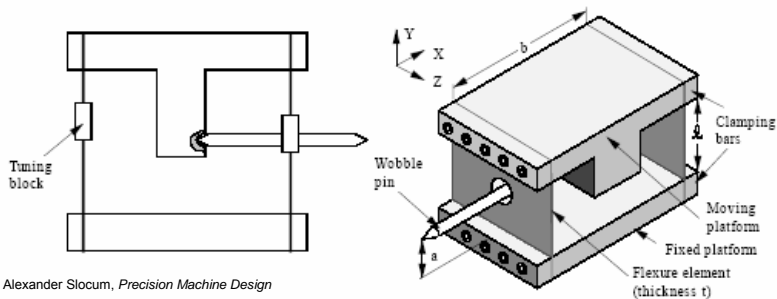
$$\theta_{spring} = \frac{\delta_{spring} x^2}{2l^2 b}$$

$$\theta_{platform} = \frac{\delta_{platform} x}{lb}$$



Types of Flexures

- 4 bar linkage



Source: Alexander Slocum, *Precision Machine Design*

- In the y direction there is a small error motion δ_y that is a function of the x motion δ_x and flexure length l :

$$\delta_y \approx \frac{\delta_x^2}{2l}$$



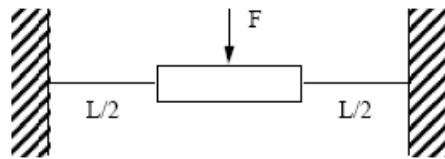
Types of Flexures

- Consider other parasitic motions mentioned earlier
- x direction stiffness is equal to two fixed-fixed beams acting together in a side by side mode
- y direction stiffness is equal to that of two columns
- Buckling effect is negligible for small motions and should be prevented by the x direction servo



Minimize Errors

- To minimize parasitic motions:
 - Symmetrical dual four bar linkage eliminates δ_y error
 - Strains along flexure's length resisted by the frame
 - Stiffness is increased: range of motion is decreased



$$\delta = \frac{FL^3}{192EI}$$

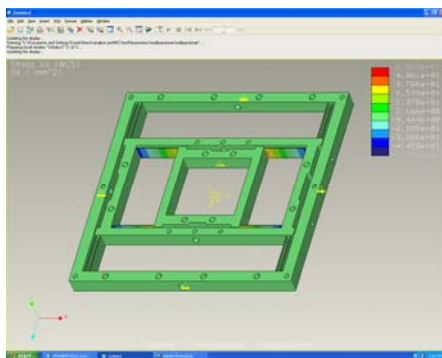
Source: Alexander Slocum, *Precision Machine Design*



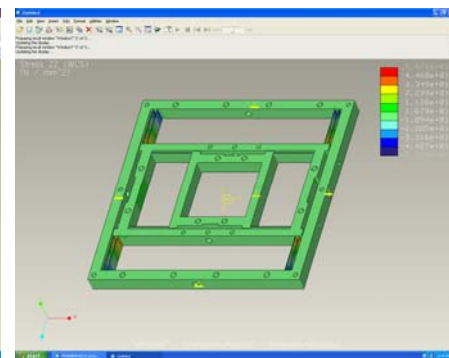
Minimize Errors

- Use a two stage (stacked) four bar linkage:

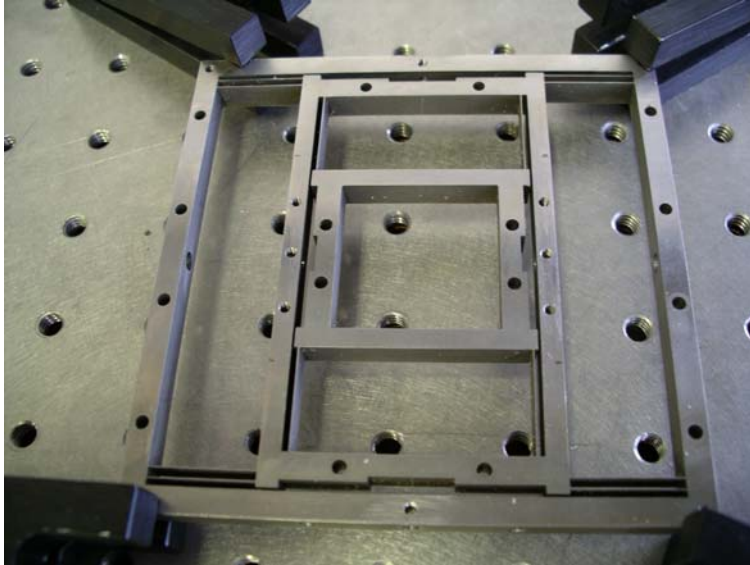
Inner Axis



Outer Axis



Stacked Axes

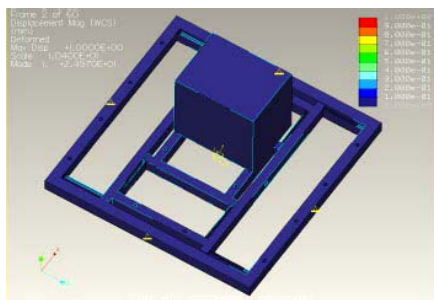


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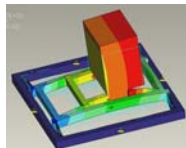
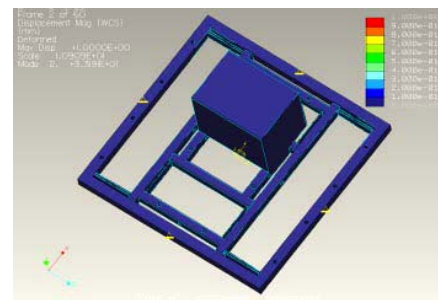
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Modal Analysis

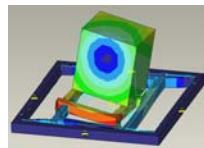
Mode 1 at 25.0 Hz



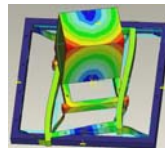
Mode 2 at 33.2 Hz



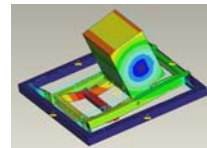
Mode 3: 319.7 Hz



Mode 4: 471.2 Hz



Mode 5: 516.5 Hz



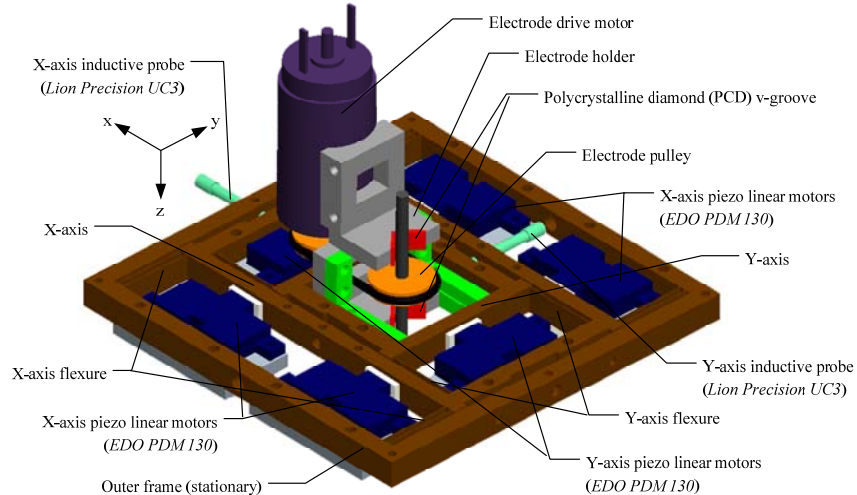
Mode 6: 642.9 Hz



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Design of Flexural X-Y Micro-EDM Head



Flexural 2-axis EDM head with piezo linear motors and non-contact inductive probes



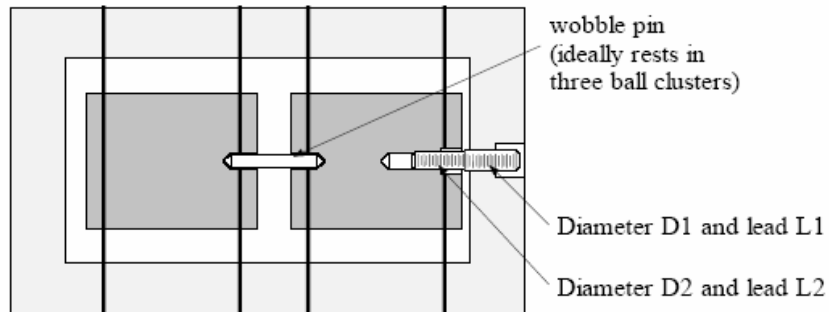
Minimize Errors

- The parasitic motion of one 4-bar cancels the parasitic motion of the second 4-bar
- Lateral and yaw stiffness will not be high, however, due to buckling effect
- Overcome by use of monolithic hourglass-type members



Minimize Errors

- A differential actuation system can be used to increase resolution
 - A wobble pin will minimize parasitic force actuation errors

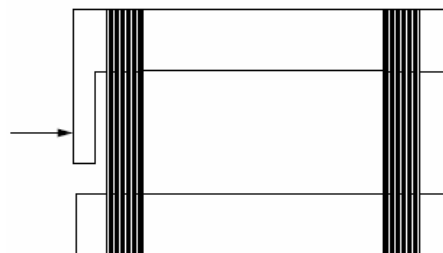


Source: Alexander Slocum, *Precision Machine Design*



Minimize Errors

- Many thin blades can be used to increase lateral stiffness and load capacity while keeping axial stiffness and stress low



Source: Alexander Slocum, *Precision Machine Design*

$$F_{load\ capacity} \approx Ntw$$

$$k_{axial\ multiblade} = \frac{L^3}{ENt^3w}$$

$$k_{vertical} = \frac{NtwE}{L}$$

$$k_{axial\ monolithic} = \frac{L^3}{E(Nt)^3w}$$



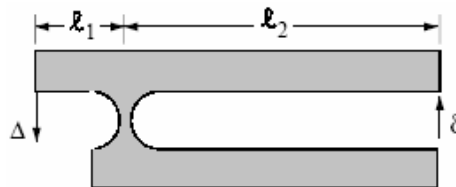
Minimize Errors

- Be careful of alignment and slip problems between the blades
- EDM process can be used to prevent these problems
- Rubber placed between the blades can increase damping
- Careful when tightening bolts, as the torque can twist the flexure



Flexural Transmission Systems

- Lever and fulcrum transmission:

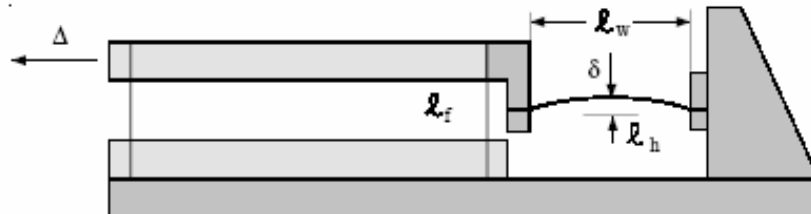


Source: Alexander Slocum, *Precision Machine Design*



Flexural Transmission Systems

- A bowed flexure used as a high reduction transmission:



- A downward motion δ causes a lateral motion Δ :

$$\Delta \approx \frac{4\delta l_h}{l_w}$$



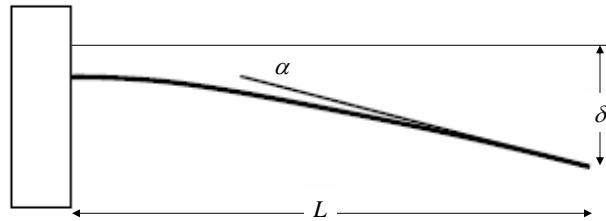
Flexural Transmission Systems

- It is possible to chain together a series of these bowed flexures at right angles to each other
 - This can yield a very high transmission ratio
 - Assume that $l_h = 2$ mm and $l_w = 20$ mm, then the transmission ratio is 5
 - In series, the ratios become 25, 125, 625... for 2, 3, 4... units respectively
- A variation to this bowed beam approach is to use two beams laid on top of each other and tied together at one end
- When the beams bend there will be differential motion along the interface between them



Angular Flexures

- The slope at the end of the beam causes an Abbe error in the beam that holds the optic which cancels the beam deflection $\delta = \alpha(2/3L)$:



$$\delta = \frac{FL^3}{3EI} \quad \alpha = \frac{FL^2}{2EI}$$

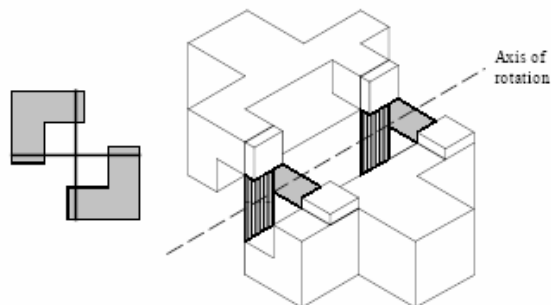


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Angular Flexures

- Cross-strip flexure for angular motion:



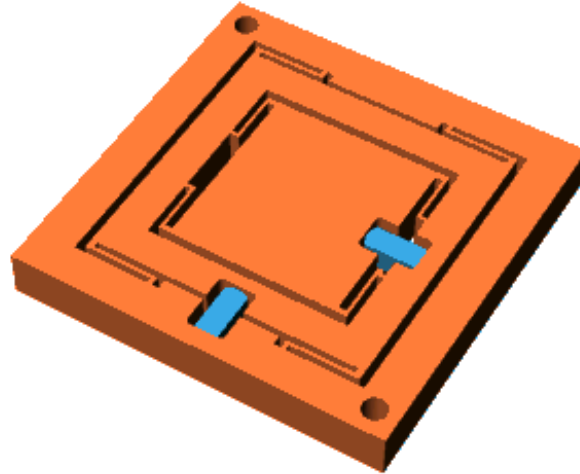
Source: Alexander Slocum, *Precision Machine Design*



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Application Examples



Source: Physikinstrumente at www.physikinstrumente.de



Piezo-Driven Linear Axis

